

TEST Παραγωντοποίηση / A' ορθιδα.

$$1. 30y^3 + 25y^2 = 5 \cdot 6 \cdot y \cdot y^2 + 5 \cdot 5 \cdot y^2 = 5y^2 \cdot (6y + 5)$$

$$2. 12x^2 + 6x = 2 \cdot 6 \cdot x \cdot x + 6x \cdot 1 = 6x \cdot (2x + 1)$$

$$3. 4a^2b + 8ab^2 - 6ab = 2 \cdot 2 \cdot a \cdot b \cdot b + 2 \cdot 4 \cdot a \cdot b \cdot b - 2 \cdot 3 \cdot a \cdot b \\ = 2ab \cdot (2a + 4b - 3)$$

$$4. 15(x-1) \cdot y + 5(x-1) \cdot w = 3 \cdot 5 \cdot (x-1) \cdot y + 5 \cdot (x-1) \cdot w \\ = 5 \cdot (x-1) \cdot (3y + w)$$

$$5. x^2 - 25 = x^2 - 5^2 = (x-5) \cdot (x+5)$$

$$6. 7a(x-1) + 14b(1-x) = 7 \cdot a \cdot (x-1) - 2 \cdot 7 \cdot b \cdot (x-1) \\ = 7 \cdot (x-1) \cdot (a - 2b)$$

$$7. 36x^2 - 9 = (6x)^2 - 3^2 = (6x-3)(6x+3)$$

$$8. 4x^2 - 16y^2 = (2x)^2 - (4y)^2 = (2x-4y)(2x+4y) \\ = (2 \cdot x - 2 \cdot 2 \cdot y)(2x + 2 \cdot 2 \cdot y) = 2 \cdot (x-2y) \cdot 2 \cdot (x+2y) \\ = 4 \cdot (x-2y) \cdot (x+2y)$$

$$9. 3a^2 - 12b^2 = 3 \cdot a^2 - 3 \cdot 4 \cdot b^2 = 3 \cdot (a^2 - 4b^2) = 3(a^2 - (2b)^2) \\ = 3(a - 2b) \cdot (a + 2b)$$

$$10. y^2 - 10y + 25 = y^2 - 2 \cdot y \cdot 5 + 5^2 = (y-5)^2$$

$$11. x^2 + x \cdot y + b \cdot x + b \cdot y = x \cdot x + x \cdot y + b \cdot x + b \cdot y \\ = x \cdot (x+y) + b \cdot (x+y) \\ = x \cdot (x+y) + b \cdot (x+y) \\ = (x+y) \cdot (x+b)$$

$$\begin{aligned}
 12. \quad x^2 - 2xy + y^2 - x + y &= (x^2 - 2xy + y^2) - (x - y) \\
 &= (x - y)^2 - (x - y) \\
 &= \underbrace{(x - y)}_{\text{mmmm}} \cdot \underbrace{(x - y)}_{\text{mmmm}} - \underbrace{(x - y)}_{\text{mmmm}} \cdot 1 \\
 &= (x - y) \cdot [(x - y) - 1] \\
 &= (x - y)(x - y - 1)
 \end{aligned}$$

$$\begin{aligned}
 13. \quad \alpha^2 \beta^2 - 4\beta^2 - \alpha^2 + 4 &= (\alpha^2 \beta^2 - 4\beta^2) - (\alpha^2 - 4) \\
 &= \beta^2 \cdot \underbrace{(\alpha^2 - 4)}_{\text{mmmm}} - \underbrace{(\alpha^2 - 4)}_{\text{mmmm}} \cdot 1 \\
 &= \underbrace{(\alpha^2 - 4)}_{\text{mmmm}} \cdot \underbrace{(\beta^2 - 1)}_{\text{mmmm}} \\
 &= (\alpha^2 - 2^2) \cdot (\beta^2 - 1^2) \\
 &= (\alpha - 2) \cdot (\alpha + 2) \cdot (\beta - 1) \cdot (\beta + 1)
 \end{aligned}$$

$$\begin{aligned}
 14. \quad 3y^2 + 24y + 48 &= \underbrace{3 \cdot y^2}_{\text{mmmm}} + \underbrace{3 \cdot 8 \cdot y}_{\text{mmmm}} + \underbrace{3 \cdot 16}_{\text{mmmm}} \\
 &= \underbrace{3}_{\text{mmmm}} \cdot (y^2 + 8y + 16) \\
 &= 3(y^2 + 2 \cdot y \cdot 4 + 4^2) \\
 &= 3(y + 4)^2
 \end{aligned}$$

$$\begin{aligned}
 15. \quad \alpha^2 + 2\alpha\beta + \beta^2 - \gamma^2 &= (\alpha^2 + 2\alpha\beta + \beta^2) - \gamma^2 \\
 &= (\alpha + \beta)^2 - \gamma^2 \\
 &= [(\alpha + \beta) - \gamma] \cdot [(\alpha + \beta) + \gamma] \\
 &= (\alpha + \beta - \gamma) \cdot (\alpha + \beta + \gamma).
 \end{aligned}$$